

# Correcting NLOS by 3D LiDAR and building height to improve GNSS single point positioning

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## Abstract

We present a novel method to detect the GNSS NLOS and correct the NLOS pseudorange measurements based on on-board sensing. This paper demonstrates the use of LiDAR scanner and a list of building heights to describe the perceived environment. To estimate the geometry and pose of the top edges of buildings (TEBs) relative to the GNSS receiver, a surface segmentation method is employed to detect the TEBs of surrounding buildings using 3D LiDAR point clouds. The top edges of the building are extracted and extended using the building height list in Skyplot to identify the NLOS-affected ones. Innovatively, the NLOS delay in pseudorange is corrected based on the detected TEBs. Weighted least squares (WLS) is used to cooperate the corrected NLOS and other pseudorange measurements. Vehicle experiments are conducted in two different urban canyons to verify the effectiveness of the proposed method in improving GNSS single point positioning (SPP) accuracy.

## 1 | INTRODUCTION

Positioning in urban environments is becoming essential due to the increasing need for autonomous vehicles. To achieve L4<sup>1</sup> autonomous driving in all scenarios, centimeter-level absolute positioning is required. The three-dimensional (3D) Light Detection and Ranging (LiDAR) is widely used in autonomous driving vehicles.<sup>2,3</sup> LiDAR, camera, and Inertial Navigation Systems (INS) only provide relative positioning. Thus, these sensors are usually integrated with the Global Navigation Satellite System (GNSS),<sup>4-7</sup> as it is one of the indispensable sources that can provide absolute positioning. A GNSS/INS/LiDAR/high-definition (HD) map integrated system can provide satisfactory localization service in sub-urban<sup>8,9</sup> areas. The suburban areas, in fact, can be regarded as GNSS-friendly areas since the GNSS receiver can receive sufficient direct signals transmitted from multi-constellation GNSS.<sup>10</sup> In urbanized cities, such as Tokyo, Hong Kong, and New York, the

signals from satellites can be reflected, blocked, and diffracted by surrounding buildings before they are received by the receiver. If the direct light-of-sight (LOS) is blocked and reflected signals from the same satellite are received, the notorious non-light-of-sight (NLOS) receptions occur. NLOS is the dominant GNSS positioning error in the cities mentioned above.<sup>11</sup> As a result, the positioning error can go up to even 100 m.<sup>12,13</sup>

According to a recent review paper,<sup>11</sup> NLOS is currently the major difficulty in using GNSS for intelligent transportation. Due to NLOS, the performance of GNSS positioning becomes highly related to environmental features, such as buildings. Utilizing the 3D building model to detect the NLOS is straightforward. NLOS can be detected with the aid of a building model and then be excluded from GNSS positioning.<sup>14,15</sup> However, the NLOS exclusion will distort the geometric distribution of the satellites. In urban canyons, the distortion results in large positioning error in the across-street

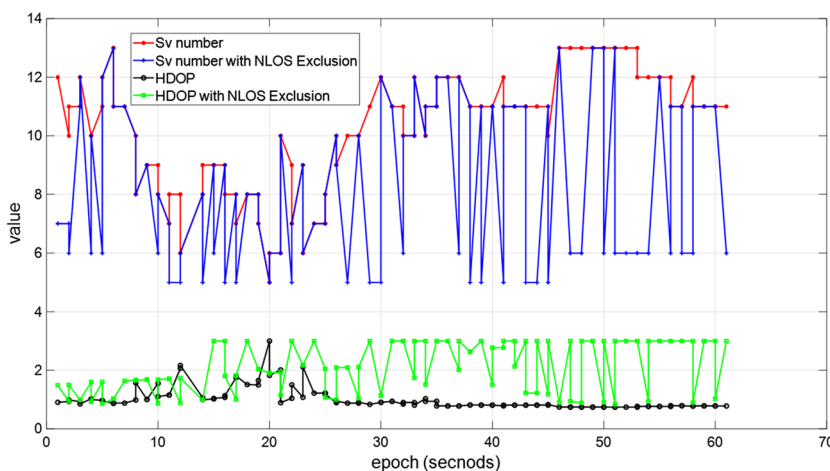
direction because only the measurements from the satellites located at the along-street direction are not excluded. Moreover, identifying NLOS measurement based on the 3D building model relies heavily on the initial guess of the GNSS receiver.<sup>16</sup>

Figure 1 shows the number of GNSS satellites (GPS and BeiDou) received by a commercial GNSS receiver in an urban canyon in Hong Kong. We can see from Figure 1 that the number of satellites is dramatically decreased after applying NLOS exclusion. The horizontal dilution of precision (HDOP) is increased (shown in Figure 1) distinctly. Thus, it is not preferable to exclude all the NLOS measurements in such an area (ie, a narrow urban canyon). A smart approach called GNSS shadow matching is proposed to match the measured satellite visibility (classifying into LOS and NLOS) with the predicted satellite visibility of hypothesized positions.<sup>17</sup> This method makes use of NLOS to improve the positioning accuracy in the across-street direction.<sup>18</sup> A likelihood-based 3D mapping aided (3DMA) GNSS method that models the measurement uncertainty to mitigate the NLOS receptions is also proposed to provide accurate positioning in the along-street direction.<sup>19</sup> Due to the complementariness of the shadow matching and the likelihood-based 3DMA GNSS, their integration has recently been studied.<sup>20</sup> Another type of range-based 3DMA GNSS methods corrects the NLOS affected measurement for GNSS positioning.<sup>21-24</sup> These methods are proposed to simulate the signals' transmission routes using the ray-tracing method.<sup>25</sup> However, the drawbacks of these ray-tracing-based 3DMA GNSS methods are the stringent requirements on (a) the accuracy of the 3D mapping database, (b) the initial guess of receiver positions, and (c) the computational power of the processors.

Instead of using only the 3D mapping data, other scanning sensors, including cameras and LiDAR, can

also be employed to sense the surrounding environments of the receiver in real-time operation. To detect the visibility of satellites, omnidirectional and fisheye cameras<sup>26-28</sup> are used to detect the skylines of buildings in the urbanized area. NLOS receptions can be detected with the detected skylines, and some improvements are obtained. However, this method can suffer from strong light or night scenarios, as computer vision is employed to detect the skylines. The constructed map of the environment using 3D LiDAR is employed to classify the visibility of satellites. Another study modeled the GNSS noise covariance by NLOS detection based on a LiDAR-constructed map.<sup>29</sup> Research incorporating a LiDAR map and a 3D city model to exclude NLOS has been conducted in the application of unmanned aerial vehicles.<sup>30</sup> However, these methods still tend to exclude the NLOS receptions from further GNSS positioning, which is not applicable in deep urban areas.

In this paper, we propose improving the GNSS single point positioning (SPP) by detecting and correcting NLOS receptions based on the environment features perceived by real-time 3D point clouds generated by 3D LiDAR. The perceived environment features refer to the surrounding buildings of the receiver in this paper. Dimension and pose of the building wall relative to GNSS receiver are calculated by the point cloud-based segmentation. Due to the limited field of view (FOV), tall buildings cannot be fully scanned. Thus, the height of the detected building wall is extended to the exact height provided by a building height list obtained from Google Earth. Then, the satellites and detected edges of buildings (TEBs) are projected into the Skyplot. To implement the projection, the globally referenced yaw angle of the vehicle is needed and is provided by an RTK GNSS/INS integrated system (SPAN-CPT). Based on the detected TEBs, NLOS

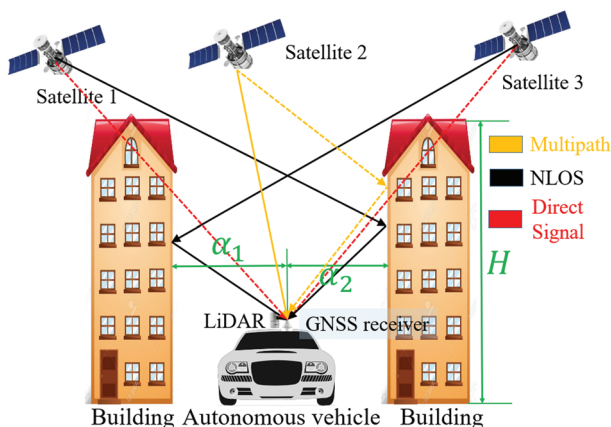


**FIGURE 1** Demonstration of number of satellite (GPS/BeiDou) measurements before and after NLOS exclusion in an urban canyon in Hong Kong. The horizontal dilution of precision (HDOP) is also given before and after (green) exclusion [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com) and [www.ion.org](http://www.ion.org)]

measurement can be identified. Previously, our team proposed an NLOS error model based on two parameters: the distance between the GNSS receiver and NLOS reflector and the elevation and azimuth angle of the satellite.<sup>12</sup> In this paper, the distance between the GNSS receiver and reflectors can be obtained by LiDAR scanner. Thus, the correction of NLOS-affected pseudorange measurements can be calculated. Finally, GNSS SPP is calculated using both the corrected NLOS measurements and LOS visible measurements.

To the best of the authors' knowledge, this is the first attempt to aid GNSS SPP by employing real-time 3D point clouds to detect and correct NLOS measurements. This is important because GNSS is usually integrated with dead-reckoning (eg, INS, odometer, visual odometry, and LiDAR odometry) for various applications. Tightly-coupled integration is one of the most popular existing solutions for the integrated navigation system. Our proposed GNSS SPP with NLOS correction can easily fit into the tightly-coupled integration scheme. In other words, it can be easily implemented in many existing navigation systems, especially those used in autonomous driving.

The remainder of this paper is structured as follows. An overview of the proposed method is given in Section 2. Section 3 discusses a method to detect TEBs from LiDAR point clouds. The coordinate transformation from LiDAR to GNSS Skyplot coordinate system is also presented in this section. In Section 4, the criterion of NLOS detection is proposed and the NLOS correction model is introduced. In Section 5, we evaluate the effectiveness of the proposed method by two vehicle experiments in two typical urban canyons in Hong Kong. Finally, conclusions are drawn in Section 6.



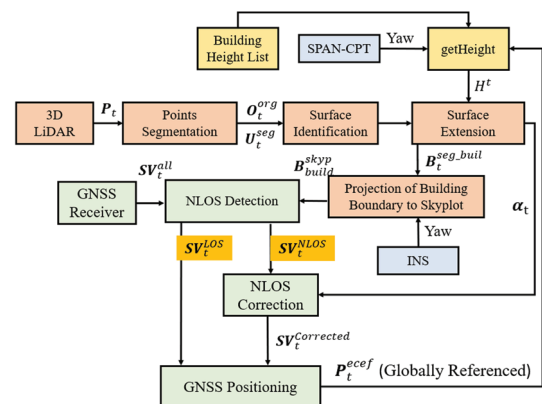
**FIGURE 2** Illustration of GNSS signal transmission routes in the urbanized area in Hong Kong. NLOS/multipath can be caused by surrounding buildings [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com) and [www.ion.org](http://www.ion.org)]

## 2 | OVERVIEW OF THE PROPOSED METHOD

In this study, we focus on the NLOS receptions caused by surrounding buildings. Figure 2 presents direct propagation routes, multipath, and potential NLOS receptions of GNSS signals. The buildings, for which height is indicated by  $H$ , can block a signal transmitted from a satellite, for example, satellite 1 in Figure 2. Meanwhile, this GNSS signal is reflected by the other nearby building and finally received by the GNSS receiver equipped on top of the autonomous vehicle, resulting in NLOS receptions. Actually, this kind of scenario is a regular case in Hong Kong. In this case, the number of satellites visible to the GNSS receiver is related to the height of nearby buildings and the distance from the receiver to the building ( $\alpha_i$  in Figure 2).

As a significant sensor for positioning and perception of autonomous driving,<sup>31</sup> 3D LiDAR is installed on the top of the car, as shown in Figure 2. In this paper, LiDAR is employed to detect the surrounding building surfaces and obtain the distance from the GNSS receiver to the building surface, and the TEBs can subsequently be identified. Then, NLOS detection and correction is implemented based on detected TEBs projected into a Skyplot, and the distance from the GNSS receiver to buildings. Finally, GNSS positioning is performed using both the corrected and healthy pseudorange measurements. Figure 3 shows the flowchart of the proposed method. The proposed method can be executed as follows:

Step I. Point cloud segmentation method is employed to detect the building surface. The pose of TEBs relative to the GNSS receiver is calculated. The distance



**FIGURE 3** Flowchart of the proposed method of GNSS SPP with NLOS correction. The inputs are the 3D LiDAR, yaw angle, building height list, and GNSS raw measurements [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com) and [www.ion.org](http://www.ion.org)]

between the GNSS receiver and the buildings can be obtained subsequently. Moreover, a building height list from Google Earth is employed to extend the detected building height to the exact height.

- Step II. The TEBs are projected into a GNSS Skyplot based on their estimated poses relative to the GNSS receiver and yaw angle provided by the SPAN-CPT (RTK GNSS/INS integrated navigation system).
- Step III. Considering satellite elevation angle, azimuth angle, signal-to-noise ratio (SNR), and TEB information (elevation and azimuth angles in Skyplot), satellites blocked by buildings are detected. Consequently, NLOS correction is implemented with an NLOS error model.
- Step IV. Implementing GNSS weighted least squares (WLS) based on the corrected pseudorange measurements and healthy pseudorange measurements.

The details of the algorithms are introduced in the following sections.

### 3 | BUILDING SURFACE DETECTION AND TRANSFORMATION

To detect the surface of the building and obtain the corresponding distances between the GNSS receiver and buildings, a point cloud segmentation method is employed.

#### 3.1 | TEBs detection and transformation

The surrounding environment is expressed as points set  $\mathbf{P}_t = \{\mathbf{p}_1, \mathbf{p}_2, \dots, \mathbf{p}_n, t\}$  at a given time  $t$ , where  $\mathbf{p}_i = (x_i, y_i, z_i)$  represents a single point in the LiDAR coordinate system. To distinguish the building surface from the unordered points set and determine the distance from the GNSS receiver to the building surface, three steps are needed: (a) segmentation of point clouds, (b) identification of buildings from segmented objects, and (c) extension of buildings top boundaries (TEBs).

The point cloud segmentation is summarized in detail in Algorithm 1. Inputs of Algorithm 1 are the points set (3D point clouds) and search radius  $r_{search}$ , which is the variable constraining the searching area in the *KD*-tree.<sup>32</sup> Outputs include the bounding box<sup>33</sup> sets ( $\mathbf{U}_t^{seg}$ ) and organized point clusters ( $\mathbf{O}_t^{org}$ ), which indicate different objects such as buildings and vehicles. The definitions of applied variables and functions in Algorithm 1 are listed as follows:

- $\mathbf{P}_t$ : input 3D point clouds.
- $\mathbf{U}_t^{seg}$ : segmented bounding box sets.
- $\mathbf{O}_t^{org}$ : segmented point clusters.
- $\mathbf{P}_t^{check}$ : a middle variable that contains checked points.
- $\mathbf{N}_i$ : a neighboring points set given a searching radius.
- $r_{search}$ : the radius of neighboring points searching area.

The *BoundingBox* mentioned in Algorithm 1 is a function to get the bounding box that represents the organized point cluster. Bounding box  $\mathbf{U}_i$  is specifically determined by a vector  $\mathbf{U}_i$  as follows:

$$\mathbf{U}_i = [x_i^c, y_i^c, z_i^c, roll_i^c, pitch_i^c, yaw_i^c, d_i^{len}, d_i^{wid}, d_i^{hei}]^T, \quad (1)$$

where  $x_i^c$ ,  $y_i^c$ , and  $z_i^c$  denote the position of the bounding box in  $x$ ,  $y$ , and  $z$  directions in the LiDAR coordinate system, respectively.  $roll_i^c$ ,  $pitch_i^c$ , and  $yaw_i^c$  denote the orientation of the bounding box in the LiDAR coordinate system.  $d_i^{len}$  is the length,  $d_i^{wid}$  is the width, and  $d_i^{hei}$  is the height of the bounding box.

The principle of Algorithm 1 is also shown in the left side of Figure 4. The discrete points represent raw 3D point clouds. After applying Algorithm 1, two clusters are detected, which are annotated by the two black 2D bounding boxes ( $\mathbf{U}_t^{seg}$ ). However, we do not know which belongs to the building class.

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#### Algorithm 1 Segmentation for points set $\mathbf{P}_t$

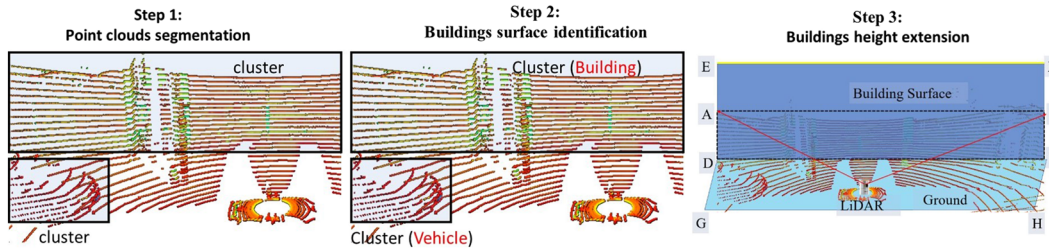
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**Input:** points set  $\mathbf{P}_t = \{\mathbf{p}_1, \mathbf{p}_2, \dots, \mathbf{p}_n, t\}$ , search radius  $r_{search}$

**Output:** Bounding box sets  $\mathbf{U}_t^{seg} = \{\mathbf{U}_1, \mathbf{U}_2, \dots, \mathbf{U}_i, \dots, \mathbf{U}_m, t\}$ , Organized point clusters  $\mathbf{O}_t^{org} = \{\mathbf{O}_1, \mathbf{O}_2, \dots, \mathbf{O}_i, \dots, \mathbf{O}_m, t\}$

- 1 create a *KD*-tree representation for the input points set  $\mathbf{P}_t$
- 2 set up an empty list to save point sets  $\mathbf{P}_t^{check}$
- 3 **for all** points  $p_i$  in  $\mathbf{P}_t$  **do**
- 4   add  $p_i$  to the points set  $\mathbf{P}_t^{check}$
- 5   **for all**  $p_i$  in  $\mathbf{P}_t^{check}$  **do**
- 6     search for the points set  $\mathbf{N}_i$  of point neighbor of  $\mathbf{p}_i$  in a sphere with radius  $r < r_{search}$
- 7     **for every** point  $\mathbf{N}_i^i$  in points set  $\mathbf{N}_i$  **do**
- 8       **if**  $\mathbf{N}_i^i$  have not been processed
- 9         add  $\mathbf{N}_i^i$  to points sets  $\mathbf{P}_t^{check}$
- 10       **end if**
- 11     **end for** the points set  $\mathbf{N}_i$
- 12 **if all** the points in  $\mathbf{P}_t^{check}$  have been processed
- 13   add  $\mathbf{P}_t^{check}$  to  $\mathbf{O}_t^{org}$  as an organized points set





**FIGURE 4** Illustration of point sets segmentation and TEBs identification, extension. Box ABCD represents the initially detected building surface. Box CDEF represents the extended building surface. Box CDGH represents the ground. The discrete points denote the point clouds from 3D LiDAR [Color figure can be viewed at wileyonlinelibrary.com and www.ion.org]

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14  add Bounding Box ( $P_t^{\text{check}}$ ) to  $U_t^{\text{seg}}$  as a bounding
box
15  reset  $P_t^{\text{check}}$  to empty
16  end if
17  end for  $P_t^{\text{check}}$ 
18  end for  $P_t$ 

```

To effectively identify the bounding box ( $U_t^{\text{seg}}$ ) representing the building surface that can result in GNSS signal reflections and subsequent NLOS receptions, a surface identification method is needed; this is summarized in detail in Algorithm 2. The objective of Algorithm 2 is to (a) identify the buildings shown in the middle side of Figure 4 and (b) extend their heights to the exact ones (right side of Figure 4). The inputs of this algorithm are  $U_t^{\text{seg}}$  and  $O_t^{\text{org}}$  obtained from Algorithm 1, and some experimentally determined thresholds.

The definitions of applied variables and functions in Algorithm 2 are listed as follows:

- $num_{\text{thres}}$ : The number of points that the cluster belongs to and the building class should contain.
- $len_{\text{thres}}$ : minimum length of a 2D bounding box that belongs to the building class.
- $hei_{\text{thres}}$ : minimum height of a 2D bounding box that belongs to the building class.
- building height list,  $H_{\text{build}}$ , receiver position  $P_r^{\text{cecf}}$ , and yaw angle,  $Yaw_r$ .

The output is the bounding box set  $B_t^{\text{seg}^{\text{buil}}}$  specifically representing the building surface. The function  $Num$  mentioned in Algorithm 2 is used to calculate the number of points in each cluster,  $O_i$ . The function  $getHeight$  is used to search the height information from a saved building height list, which contains the height information. To determine the actual height of the identified building surface,  $P_r^{\text{cecf}}$ ,  $U_i$ , and  $Yaw_r$  are also needed.  $P_r^{\text{cecf}}$  indicates the GNSS position given by the previous-epoch positioning result. Relative position between GNSS receiver and detected building can be obtained from  $U_i$ .

For each bounding box,  $B_i$ , the distance,  $\alpha_i$ , from the receiver to the detected building surface can be calculated as follows:

$$\alpha_i = \sqrt{((x_i^c)^2 + (y_i^c)^2 + (z_i^c)^2)}. \quad (2)$$

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**Algorithm 2** Building surface identification from bounding box sets and height extension of TEBs

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**Input:** Bounding Box sets  
 $U_t^{\text{seg}} = \{U_1, U_2, \dots, U_i, \dots, U_m, t\}$ , Organized point clusters  
 $O_t^{\text{org}} = \{O_1, O_2, \dots, O_i, \dots, O_m, t\}$ , point number threshold  
 $num_{\text{thres}}$ , length threshold  $len_{\text{thres}}$  and height threshold  $hei_{\text{thres}}$ , building height list  $H_{\text{build}}$ , receiver position  $P_r^{\text{cecf}}$ , yaw angle  $Yaw_r$ .

**Output:** Bounding Box set represents building surfaces  $B_t^{\text{seg}^{\text{buil}}} = \{B_1, B_2, \dots, B_i, \dots, B_m, t\}$

```

1  set up an empty clusters list  $B_t^{\text{seg}^{\text{buil}}}$  to save bounding box
2  for all bounding box  $U_i$  in  $U_t^{\text{seg}}$  do
3    if  $Num(O_i) > num_{\text{thres}}$ 
4       $U_i \leftarrow [x_i^c, y_i^c, z_i^c, roll_i^c, pitch_i^c, yaw_i^c, d_i^{\text{len}}, d_i^{\text{wid}}, d_i^{\text{hei}}]$ 
5      if  $d_i^{\text{len}} > len_{\text{thres}}$  and  $d_i^{\text{hei}} > hei_{\text{thres}}$ 
6         $d_i^{\text{hei}} \leftarrow getHeight(H_{\text{build}}, P_r^{\text{cecf}}, U_i, Yaw_r)$ 
7         $B_i \leftarrow U_i$ 
8      end if
9    end if
10  end for  $U_t^{\text{seg}}$ 

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Thus, the bounding box with extended height representing the building surface can be identified with Algorithm 2. The height of the bounding box representing building surface can be extended to the real one. The bounding box is extended from rectangle ABCD to rectangle CDEF, as can be seen in the right side of Figure 4. Then, the parameters of the TEBs for the bounding box,  $B_i$ , corresponding to the building surface are denoted by line

segment  $\overline{EF}$ , denoted as  $\mathbf{B}_{build}^{3d}$ , the matrix of the building boundary. To represent the building boundary, two points, E and F, are required.  $\mathbf{B}_{build}^{3d}$  is structured as follows:

$$\mathbf{B}_{build}^{3d} = \begin{bmatrix} x_{3dE} & y_{3dE} & z_{3dE} \\ x_{3dF} & y_{3dF} & z_{3dF} \end{bmatrix}. \quad (3)$$

### 3.2 | Coordinate transformation

To implement the algorithm for NLOS detection and subsequent correction, satellite visibility must be determined based on the extended TEBs. Thus, the relative poses of the GNSS receiver to satellites and to building surfaces need to be transformed into the same representation, the Skyplot. In each epoch, information from satellites, including azimuth, elevation angles, and SNR, can be obtained from the GNSS receiver. Part of the satellite information can be represented as  $\mathbf{SV}_t^{all} = \{\mathbf{SV}_1, \mathbf{SV}_2, \dots, \mathbf{SV}_i, \dots, \mathbf{SV}_n\}$ .  $n$  represents the number of satellites received.  $\mathbf{SV}_i$  represents the information for satellite  $i$ , and  $\mathbf{SV}_i = \{az_i, el_i, SNR_i, \rho_i\}$ .  $az_i$  denotes the satellite azimuth angle.  $el_i$  represents satellite elevation angle.  $SNR_i$  indicates satellite SNR, and  $\rho_i$  denotes the pseudorange measurement.

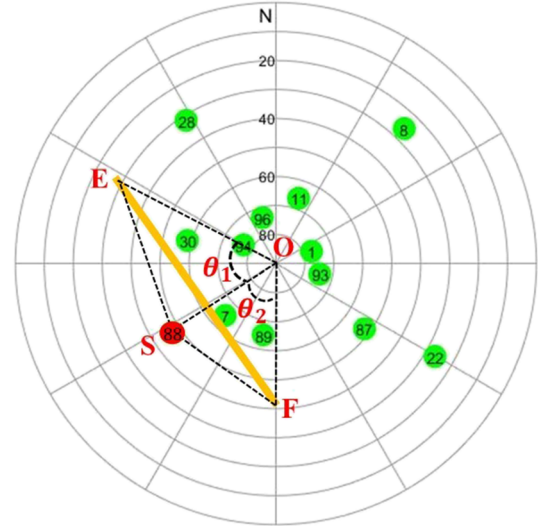
Satellite positions can be easily indicated in the Skyplot, which is a two-dimensional coordinate based on corresponding elevation and azimuth angles. A transformation matrix should be employed for TEBs transformation from a 3D coordinate to a 2D coordinate. The transformation is conducted as per the following equation.

$$\mathbf{B}_{build}^{skyp} = \mathbf{B}_{build}^{3d} \mathbf{G}_T^{build}, \quad (4)$$

where  $\mathbf{B}_{build}^{3d}$  denotes the matrix of building boundary presented in the previous sub-section.  $\mathbf{G}_T^{build}$  is a  $3 \times 2$  transformation matrix.  $\mathbf{B}_{build}^{skyp}$  denotes the boundary matrix ( $2 \times 2$ ) in the Skyplot structured as follows:

$$\mathbf{B}_{build}^{skyp} = \begin{bmatrix} x_{skypE} & y_{skypE} \\ x_{skypF} & y_{skypF} \end{bmatrix}. \quad (5)$$

After the transformation, satellites and building surface boundaries can be presented in the same coordinate frame, the Skyplot, as shown in Figure 5. The bounding box set  $\mathbf{B}_t^{seg^{buil}} = \{\mathbf{B}_1, \mathbf{B}_2, \dots, \mathbf{B}_i, \dots, \mathbf{B}_m, t\}$  can be transformed into  $\mathbf{B}_t^{skyp} = \{\mathbf{B}_1^{skyp}, \mathbf{B}_2^{skyp}, \dots, \mathbf{B}_i^{skyp}, \dots, \mathbf{B}_m^{skyp}, t\}$ , where  $\mathbf{B}_i^{skyp}$  indicates the  $i$ th boundary in the Skyplot. Moreover, the distance list representing the distances from the GNSS receiver to the detected surfaces can also



**FIGURE 5** Skyplot of GNSS satellites and detected TEBs. The numbers inside the small circles indicate satellites and corresponding PRNs. The satellite 88 is the NLOS and the rest are LOS satellites. Line segment  $\overline{EF}$  indicates the TEBs [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com) and [www.ion.org](http://www.ion.org)]

be obtained as  $\alpha_t^{seg^{buil}} = \{\alpha_1, \alpha_2, \dots, \alpha_i, \dots, \alpha_m, t\}$ , where  $\alpha_i$  is associated with  $\mathbf{B}_i^{skyp}$ . Line segment  $\overline{EF}$  represents the building surface boundary as shown in Figure 4. Then, the azimuth and the elevation angles for points E and F can be calculated in the Skyplot.

## 4 | IMPROVED GNSS POSITIONING WITH NLOS CORRECTION

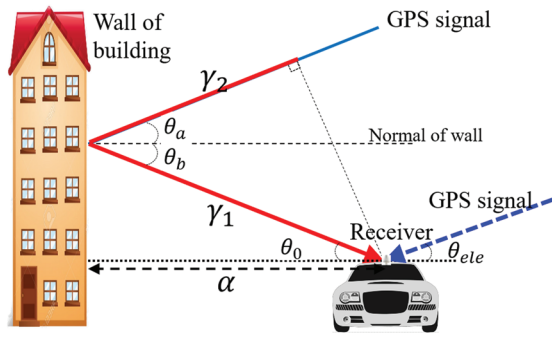
In this section, an NLOS error model is presented first. Then, the NLOS detection criterion is proposed based on the detected TEBs, satellite elevation angle, azimuth angle, and SNR. NLOS error correction is then implemented. Finally, GNSS positioning is conducted by applying the WLS method using the LOS and corrected NLOS pseudorange measurements.

### 4.1 | NLOS correction based on detected building boundary

In terms of the measurements from the GNSS receiver, each pseudorange measurement,  $\rho_n$ , is written as follows.<sup>34</sup>

$$\rho_n = R_n + c(\delta t^r - \delta t_n^{sv}) + I_n + T_n + \varepsilon_n, \quad (6)$$

where  $R_n$  is the geometric range between the satellite and the GNSS receiver.  $\delta t_n^{sv}$  denotes the satellite clock bias.  $\delta t^r$  indicates the receiver clock bias.  $I_n$  represents the ionospheric delay distance;  $T_n$  indicates the tropospheric delay distance.  $\varepsilon_n$  represents the errors caused by the



**FIGURE 6** NLOS correction model. The signal is reflected by the building and subsequently received by receiver<sup>12</sup> [Color figure can be viewed at wileyonlinelibrary.com and www.ion.org]

multipath effects, NLOS receptions, receiver noise, and antenna delay. In this paper, we focus on mitigating the NLOS errors caused by surrounding buildings.

The NLOS error model proposed in Hsu<sup>12</sup> is expressed in Figure 6. The expected signal transmission route is expressed as a dashed blue line in Figure 6.  $\alpha$  represents the distance from the receiver to the building.  $\theta_{ele}$  represents the elevation angle of the GNSS signal. We assume that:

1. The building is vertical to the ground.
2. GNSS signal reflection satisfies the law of reflection.

Thus, we can get  $\theta_a = \theta_b$ . Moreover, the direction of real signal transmission is parallel to the direction of expected signal transmission. Finally, we have  $\theta_a = \theta_b = \theta_0 = \theta_{ele}$ . The route distance difference,  $\gamma$ , between the reflected signal and the expected signal is indicated as follows:

$$\gamma = \gamma_1 + \gamma_2, \quad (7)$$

$$\gamma_1 = \alpha \sec \theta_{ele}, \quad (8)$$

$$\gamma_2 = \gamma_1 \cos(2\theta_{ele}). \quad (9)$$

Thus, the NLOS error can be calculated based on the azimuth angle, elevation angle, and the distance from the receiver to the building causing the reflection. In general, two steps are needed to proceed with the NLOS correction: NLOS detection and NLOS error calculation. The process of NLOS correction is summarized in detail in Algorithm 3.

### Algorithm 3 NLOS detection and correction

**Input:** Satellites information set  $SV_t^{all} = \{SV_1, SV_2, \dots, SV_i, \dots, SV_n\}$ , building boundary matrix  $B_t^{skyp} = \{B_1^{skyp}, B_2^{skyp}, \dots, B_i^{skyp}, \dots, B_m^{skyp}, t\}$ , distance

list  $\alpha_t^{seg^{bul}}$ , area threshold  $S_{threshold}$ , SNR threshold  $SNR_{threshold}$ , threshold of boundary uncertainty  $\theta_{thres}$

**Output:** corrected satellite information set after NLOS identification:

$SV_t^{cor} = \{SV_1^{cor}, SV_2^{cor}, \dots, SV_i^{cor}, \dots, SV_j^{cor}\}$ . LOS satellite set  $SV_t^{los} = \{SV_1^{los}, SV_2^{los}, \dots, SV_i^{los}, \dots, SV_k^{los}\}$ .

```

1 for all boundary  $B_i^{skyp}$  in  $B_t^{skyp}$  do
2   for all satellites  $SV_i$  in  $SV_t^{all}$  do
3     estimate  $\theta_1, \theta_2$  as shown in Fig. 5
4     Get triangle area  $S_{SEO}$  of triangle SEO
5     from  $B_i^{skyp}$ 
6     Get triangle area  $S_{SFO}$  of triangle SFO
7     from  $B_i^{skyp}$ 
8     Get triangle area  $S_{SEF}$  of triangle SEF
9     from  $B_i^{skyp}$ 
10    Get triangle area  $S_{EOF}$  of triangle EOF
11    from  $B_i^{skyp}$ 
12     $S = S_{SEO} + S_{SFO} + S_{SEF} - S_{EOF}$ 
13    if  $(SNR_i > SNR_{threshold})$  or  $(\theta_1 < \theta_{thres})$  or
14     $(\theta_2 < \theta_{thres})$ 
15      break
16    if  $S > S_{threshold}$  and  $((\theta_1 + \theta_2) < \angle EOF < 180^\circ$ 
17       $SV_i^{los} \leftarrow SV_i$  //LOS
18    else //NLOS
19       $SV_i \leftarrow \{az_i, el_i, SNR_i, \rho_i\}$ 
20       $SV_i(\rho_i) \leftarrow SV_i(\rho_i) - (\gamma_1 + \gamma_2) // \alpha_i$  from
21       $\alpha_t^{seg^{bul}}$ 
22       $SV_i^{cor} \leftarrow SV_i$ 
23    end if
24  end for satellites set  $SV_t^{all}$ 
25 end for boundary set  $B_t^{skyp}$ 

```

The inputs of Algorithm 3 include satellite information,  $SV_t^{all}$ , building surface boundary information,  $B_t^{skyp}$ , distance list,  $\alpha_t^{seg^{bul}}$ , and some experimentally determined thresholds. The definitions of applied variables and functions in Algorithm 3 are listed as follows:

- $S_{threshold}$ : Used to determine whether the satellite is inside the triangle. For example, if satellite 88 is inside triangle EOF.
- $SNR_{threshold}$ : if the SNR for a certain satellite is more than this threshold, we treat it as LOS.
- $\theta_{thres}$ : threshold of boundary uncertainty.

The outputs are the corrected satellite information set  $SV_t^{cor}$  and LOS satellite set  $SV_t^{los}$ . First, geometry angles  $\theta_1$  ( $\angle EOS$ ) and  $\theta_2$  ( $\angle FOS$ ) shown in Figure 5 are

estimated. Then areas of triangles  $S_{SEO}$ ,  $S_{SFO}$ ,  $S_{SEF}$ , and  $S_{EOF}$  are calculated and  $S$  can be estimated subsequently. Second, GNSS measurements whose SNR is larger than  $SNR_{threshold}$  will not be excluded, as signals with strong SNR are not considered to be reflected by buildings.

Satellites whose positions are quite near the extended edge beam ( $\theta_1 < \theta_{thres}$  or  $\theta_2 < \theta_{thres}$ ) also should not be excluded, such as satellite 7 in Figure 5; thus, the angle threshold  $\theta_{thres}$  is set. To avoid a faulty exclusion, a heuristically determined threshold  $S_{threshold}$  is set. Satellites whose positions are quite near the TEBs of building surfaces should not be identified as NLOS. This can be determined by comparing  $S$  and  $S_{threshold}$ , such as from satellite 7 in Figure 5. Finally, the pseudorange measurements from NLOS receptions can be corrected using the NLOS error model in Equation 7.

In this case, these NLOS satellites can be detected and corresponding pseudorange measurements are corrected.

## 4.2 | GNSS positioning based on corrected and healthy pseudorange measurements

Measurements with low elevation angle are more likely to be contaminated GNSS signals in urban canyons, such as multipath or NLOS, due to reflection, blockage, and diffraction. Thus, a proper threshold must be set to exclude the unhealthy measurements. For satellite  $SV_i$ , if  $ele_i$  is less than  $ele_{thres}$ , it should be excluded from GNSS positioning. Pseudorange measurements in  $\mathbf{SV}_i^{cor}$  and  $\mathbf{SV}_i^{los}$  will be employed for the GNSS positioning calculation.

The clock bias between the GNSS receiver and satellites is usually represented by the pseudorange measurements. The equation linking the receiver position and satellite can be structured as per the following equation using the least squares (LS) method:

$$\hat{\mathbf{x}} = (\mathbf{G}^T \mathbf{G})^{-1} \mathbf{G}^T \boldsymbol{\rho}, \quad (10)$$

where  $\mathbf{G}$  represents the observation matrix and is structured by unit LOS vectors between the GNSS receiver position and satellite position.  $\hat{\mathbf{x}}$  indicates the estimated receiver position, and  $\boldsymbol{\rho}$  denotes the pseudorange measurements.

To better represent the quality of each measurement based on the information measured by the receiver, the weightings of each satellite are needed. The weightings for each satellite are calculated using the formulation in Herrera et al.<sup>35</sup> by integrating the SNR and satellite elevation. Finally, the GNSS receiver position can be estimated using the WLS method as:

$$\hat{\mathbf{x}} = (\mathbf{G}^T \mathbf{W} \mathbf{G})^{-1} \mathbf{G}^T \mathbf{W} \boldsymbol{\rho}. \quad (11)$$

The weighting is given as follows<sup>35</sup>:

$$\mathbf{W}^{(i)}(ele_i, SNR_i) = \frac{1}{\sin^2 ele_i} \left( 10^{-\frac{(SNR_i - T)}{a}} \left( \left( \frac{A}{10^{-\frac{(F-T)}{a}}} - 1 \right) \frac{(SNR_i - T)}{F - T} + 1 \right) \right), \quad (12)$$

where  $\mathbf{W}^{(i)}(ele_i, SNR_i)$  denotes the weighting for satellite  $\mathbf{SV}_i$ . The parameter  $T$  indicates the threshold of SNR and is equal to  $SNR_{threshold}$ . Parameters  $a$ ,  $A$ , and  $F$  in 12 are experimentally determined. The weighting matrix  $\mathbf{W}$  is a diagonal matrix constituted by the weightings  $\mathbf{W}^{(k)}(ele_i, SNR_i)$ .

## 5 | EXPERIMENTAL RESULTS AND DISCUSSIONS

To evaluate the performance of the proposed method, two experiments conducted in two separate scenarios are presented in this section. First, the experimental setup is introduced in Section 5.1. Experimental validations in two typical urban canyons are presented in Sections 5.3 and 5.4, respectively. The relationship between the satellite elevation angle and NLOS error is presented in Section 5.4 before the discussion is given in Section 5.5.

### 5.1 | Experiment setup

Experiments are conducted in two typical urban canyons (urban canyon 1 and urban canyon 2) in Hong Kong and the experimental scenes are shown in Figure 7. The Skymask in the right-hand side demonstrates the degree of urbanization.

In both experiments, a u-blox M8T receiver is used to collect raw GPS and BeiDou measurements. A 3D LiDAR sensor, Velodyne 32, is employed to provide the real-time 3D point clouds scanned from the surroundings. Both the u-blox M8T receiver and the 3D LiDAR are installed on the top of an experimental vehicle that can be seen in the left-hand side of Figure 7. The data were collected at a frequency of 1 Hz for GNSS and 10 Hz for the 3D LiDAR.

In addition, the NovAtel SPAN-CPT, GNSS RTK/INS (fiber optic gyroscopes) integrated navigation system is used to provide the ground truth of positioning. All the data are collected and synchronized using the Robot Operation System (ROS).<sup>36</sup> Moreover, the coordinate systems of all the sensors are calibrated before the experiments.





**FIGURE 7** The sensors setup of the vehicle and tested environment: GNSS and LiDAR sensors are installed on the top of the vehicle shown in the left side of the figure. The two tested urban scenarios are shown in the middle of the figures. The Skyplot of the two experiments is shown in the right side of the figure [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com) and [www.ion.org](http://www.ion.org)]

The parameters used in this paper, which are experimentally determined, are shown in Table 1. Three GNSS positioning methods are compared:

1. WLS: GNSS positioning with the WLS.
2. WLS-NE: WLS with NLOS exclusion.
3. WLS-NC: WLS with NLOS correction.

## 5.2 | Evaluation of the proposed method in urban canyon 1

Figure 8 and Table 2 show the positioning results comparison of the conventional WLS, WLS-NE, and the proposed method.

As can be seen from Figure 8, the total satellite numbers fluctuate between 5 and 13, with a mean satellite number of 10 during the experiment. With the aid of the proposed NLOS correction method, the positioning performance is improved at most of the epochs, which is indicated by the blue curve in the bottom panel of Figure 8. 30.29 m of mean positioning error and 19.86 m of standard deviation were obtained using the WLS method without any NLOS exclusion or correction. After the NLOS exclusion (all the NLOS are excluded), the mean error goes up to 35.25 m. The main reason for this increase is due to the distortion of the satellite geometric distribution. In other words, the HDOP increases accordingly. According to the experiment,

**TABLE 1** Parameter values used in this paper

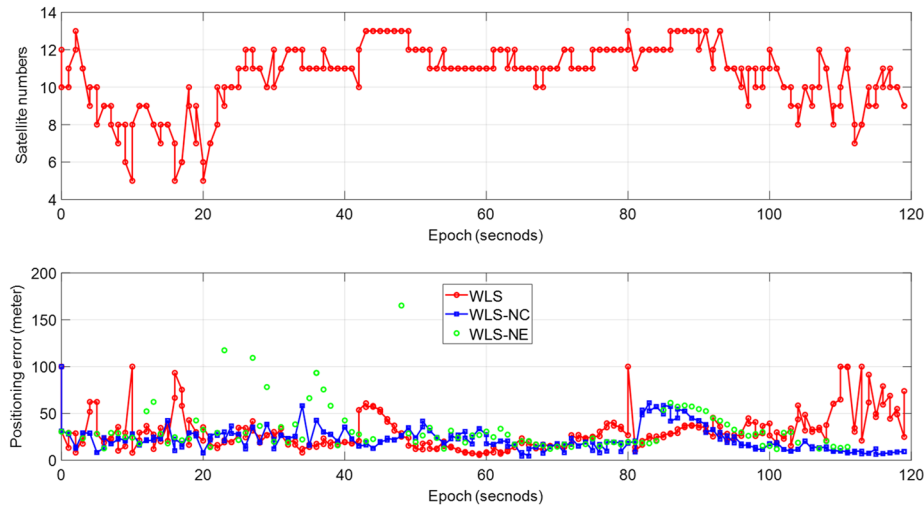
Parameters	$S_{threshold}$	$SNR_{threshold}$	$ele_{thres}$	$\theta_{thres}$
Value	10	45 dB-Hz	20°	5°
Parameters	a	A	F	
Value	30	32	10	

approximately two to six satellites are classified as NLOS due to the blockage from surrounding buildings. Therefore, the availability of GNSS positioning is decreased to about 92.5% due to the lack of satellites (at least five satellites are needed for the GPS/BeiDou-based positioning calculation). The positioning error decreases to 22.86 m using the proposed NLOS correction method. Moreover, the availability of GNSS positioning is also guaranteed. This result shows that the proposed NLOS correction model can obtain improved GNSS positioning performance.

## 5.3 | Evaluation of the proposed method in urban canyon 2

Figure 9 and Table 3 show the positioning results comparison for all three methods.

As can be seen from Figure 9, the total satellite numbers fluctuate between 8 and 15 with a mean satellite number of 11 during the experiment. With the aid of the proposed NLOS correction method, the positioning performance is improved through almost all the experiment. 42.15 m of mean positioning error and 21.29 m of standard deviation are obtained using the WLS method without any NLOS exclusion or correction. After the NLOS exclusion (all the NLOS are excluded), the mean error goes up to 47.74 m. According to the experiment, approximately three to seven satellites are classified as NLOS due to the blockage from surrounding buildings. Therefore, the availability of GNSS positioning is decreased to 88.69%. The mean positioning error is decreased to 26.7 m using the proposed NLOS correction method. Moreover, the availability of GNSS positioning is also guaranteed. Interestingly, we find that the variation trends of positioning error using two separate solutions are quite similar throughout the experiment.



**FIGURE 8** Positioning error of the GNSS before and after adding the NLOS correction, and NLOS exclusion in the urban canyon 1. The top panel indicates the satellite numbers. The bottom panel shows the positioning error: dotted curve with small circles indicates the positioning error using WLS, dotted curve with small squares denotes the positioning based on proposed NLOS correction. The discrete green circles show the result of using WLS-NE [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com) and [www.ion.org](http://www.ion.org)]

**TABLE 2** Positioning performance of the two methods in urban canyon 1 (in the unit of meter)

All Data	WLS	WLS-NE	WLS-NC
Mean error	30.29	35.25	22.86
Std	19.86	57.49	13.17
Availability	100%	92.5%	100%

## 5.4 | Analysis of satellite elevation angles versus NLOS errors

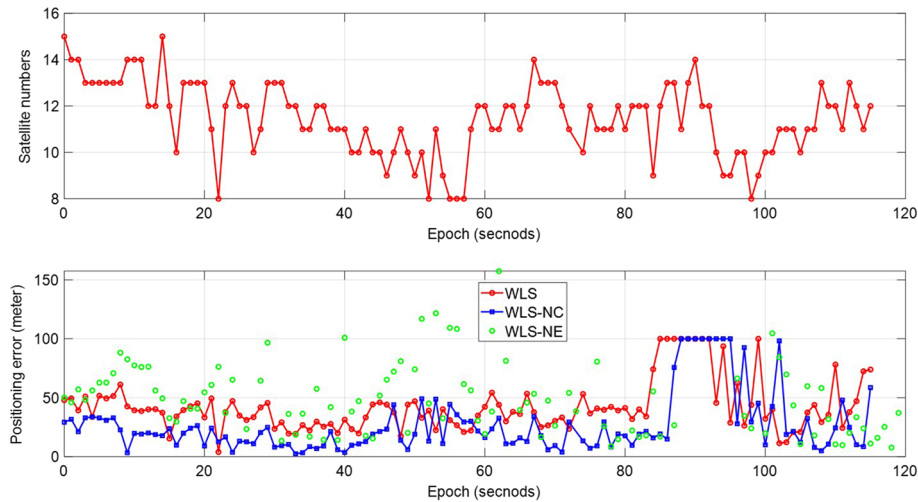
Our previous work<sup>12</sup> shows that the potential NLOS error is positively correlated to the satellite elevation angle. In other words, the NLOS satellite with higher elevation can cause larger GNSS signal transmission delay. To show the relationship of GNSS positioning error and satellite elevation angle, we apply a manual correction to the collected data. Only satellites whose elevation angles are in a certain elevation angle range are corrected. The objective is to analyze the percentages of NLOS errors contributed by each elevation angle range of satellites.

Table 4 shows the results of three separate NLOS correction tests of urban canyon 1. Three satellite elevation angle ranges are given. If satellites 2, 5, and 24 are corrected (elevation angles between  $20^\circ$  and  $36^\circ$ ), 5.5 m of improvement are obtained with a mean positioning error of 24.79 m. More than half of the results possess errors less than 15 m. If satellites 29 and 88 are corrected (elevation angles between  $36^\circ$  and  $54^\circ$ ), 1.65 m of improvement are obtained with a mean positioning error of 28.64 m. Only 17.01% of the results possess errors less than 15 m. There is almost no improvement if only satellite 13 is corrected whose elevation angle is between  $54^\circ$  and  $72^\circ$ .

Table 5 shows the results of three separate NLOS correction tests for urban canyon 2. First, if satellites 8, 17, 22, and 28 (elevation angles between  $18^\circ$  and  $36^\circ$ ) are corrected with the proposed method, the mean positioning error is decreased from 42.15 to 29.93 m compared with the WLS method. 12.22 m of improvement is obtained. Interestingly, the corresponding standard deviation also increases slightly. Approximately 79.64% of the positioning results have an error which is less than 30 m. Second, only one satellite, satellite 88, possesses an elevation angle between  $36^\circ$  and  $54^\circ$  and is NLOS. A slight improvement is introduced after the correction with a mean positioning error of 41.95 m and a standard deviation of 21.80 m. 0.2 m of improvement is obtained. Moreover, the percentage of positioning results that is more than 40 m is similar to the results from WLS. Thirdly, two satellites, satellites 30 and 99, have an elevation between  $54^\circ$  and  $72^\circ$ . A slight improvement (0.14 m) is obtained with the proposed NLOS corrections. The corresponding percentage is similar to the result from the NLOS correction of elevation range  $36^\circ$  to  $54^\circ$ . In summary, the NLOS satellites with lower elevation ( $18^\circ$  to  $36^\circ$ ) introduce larger positioning errors, compared with the NLOS satellites with higher elevation ( $36^\circ$  to  $72^\circ$ ).

## 5.5 | Discussion

- When comparing results from urban canyons 1 and 2, we find that the improvement in urban canyon 2 is more distinct (from 42.15 m to 26.70, 36.7% total improvement) than that in urban canyon 1 (from 30.29 m to 22.86, 24.5% total improvement).



**FIGURE 9** Positioning error of the GNSS before and after adding the NLOS correction in the urban canyon 2. The top panel indicates the satellite numbers. The bottom panel shows the positioning error: dotted curve with small circles indicates the positioning error using WLS, dotted curve with small squares denotes the positioning based on proposed NLOS correction. The discrete green circles show the result of using WLS-NE [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com) and [www.ion.org](http://www.ion.org)]

**TABLE 3** Positioning performance of the two methods in urban canyon 2 scenario (in the unit of meter)

All Data	WLS	WLS-NE	WLS-NC
Mean error	42.15	47.74	26.70
Std	21.29	29.34	24.32
Availability	100%	88.69%	100%

**TABLE 4** Positioning performance of WLSP-NC with manual satellite correction (in the unit of meter) in urban canyon 1

All Data	Elevation (20°~36°)	Elevation (36°~54°)	Elevation (54°~72°)
Mean error	24.79	28.64	30.1
Std	17.18	15.8	16.24
Percentage (<15 m)	51.62%	17.01%	16.69%
Percentage (<30 m)	84.66%	43.80%	40.43%
Percentage (>40 m)	10.46%	25.70%	29.57%
Improvement	5.5	1.65	0.19
NLOS satellites PRN	2,5,24	29,88	13

2. The remaining GNSS positioning errors are still 22.86 meters in urban canyon 1 and 26.70 m in urban canyon 2. The major reason behind this is that the potential GNSS multipath contributes to the remaining error. On the other hand, the performance of the NLOS correction relies on the performance of distance  $\alpha_i$  (from GNSS receiver to the reflector) estimation, as the signal from the NLOS satellite can be reflected by different buildings. As shown in Figure 10, the NLOS can be caused by both building A and building B (reflector), thus causing different

$\alpha_i$ . The proposed NLOS correction method can misidentify the reflector in some situations. In this case, this misidentification can result in positioning error. Thus, the reflector detection will be studied in future work to improve the performance of the proposed NLOS correction method.

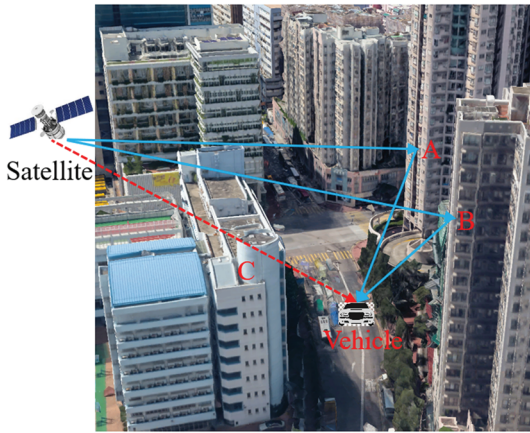
3. According to our previous research,<sup>37</sup> dynamic objects (such as a double-decker bus) on the road can also cause NLOS receptions. The effects from these dynamic objects are not modeled, which can also contribute to the remaining GNSS positioning error.
4. Performance sensitivity of the proposed method against building height errors:

The proposed method employs the building height list to extend the detected TEBs to the exact height. We implemented an offline simulation to analyze the performance sensitivity of the proposed method against building height errors. We collected 6 hours of satellite ephemeris data and did the LOS/NLOS classification based on 3D building models in Hong Kong. The building models are manually added with height noise which is subject to Gaussian distribution ( $\mathcal{N}(\mu, \delta^2)$ ). The offline processing setup is as follows:

1. Applied satellites: GPS/BeiDou/GLONASS/Galileo.
2. Ground truth for LOS/NLOS classification: the LOS/NLOS classification based on original 3D building models are treated as ground truth.
3. Accuracy of LOS/NLOS classification: detected NLOS satellite number denoted by  $N_{NLOS}^{Detected}$ , ground truth number of NLOS satellites denoted by  $N_{NLOS}^{Label}$ . Accuracy ( $P_s$ ) is calculated by  $P_s = N_{NLOS}^{Detected} / N_{NLOS}^{Label} * 100\%$ .

**TABLE 5** Positioning performance of WLSP-NC with manual satellite correction (in the unit of meter) in urban canyon 2

All Data	Elevation (20°~36°)	Elevation (36°~54°)	Elevation (54°~72°)
Mean error	29.93	41.95	42.01
Std	24.62	21.80	21.81
Percentage (<15 m)	51.32%	7.96%	8.03%
Percentage (<30 m)	79.64%	43.36%	39.29%
Percentage (>40 m)	15.04%	28.32%	30.36%
Improvement	12.22	0.2	0.14
NLOS satellites PRN	8, 17, 22, 28	88	30, 99



**FIGURE 10** Illustration of multiple NLOS signal transmission routes. The direct route from GNSS satellite to the vehicle is blocked by building C. However, the signal can be reflected by building A or building B. As a result, the vehicle can receive the GNSS signal as well [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com) and [www.ion.org](http://www.ion.org)]

**TABLE 6** Performance sensitivity of proposed method against building height errors

Yaw Bias	Mean NLOS Detection Accuracy, %	Std, %
$N(0, (2^\circ)^2)$	99.07	1.72
$N(0, (4^\circ)^2)$	97.81	2.74
$N(0, (6^\circ)^2)$	96.69	3.56
$N(0, (8^\circ)^2)$	95.47	4.46

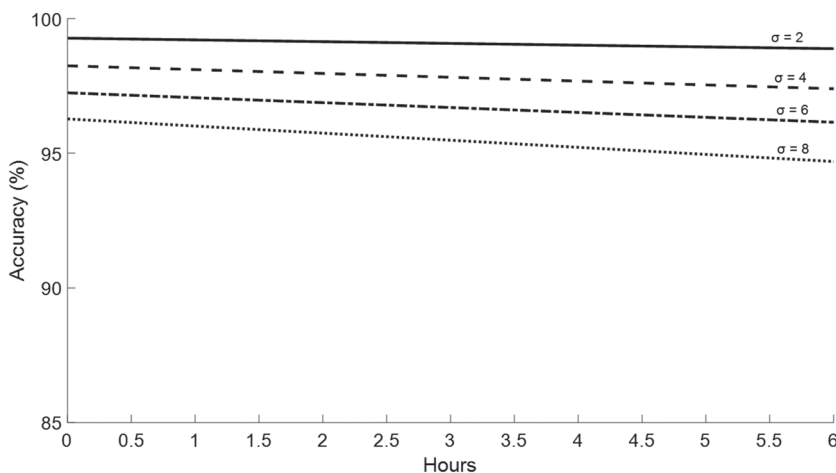
**TABLE 7** Performance sensitivity of proposed method against yaw errors in urban canyon 2 dataset

Yaw Bias	NLOS Detection Accuracy, %	Mean Positioning Error, m	Std
$N(0, (1^\circ)^2)$	100	26.70	24.32
$N(0, (2^\circ)^2)$	98.2	29.56	24.75
$N(0, (4^\circ)^2)$	95.43	30.41	24.93
$N(0, (6^\circ)^2)$	93.01	31.39	25.51
$N(0, (8^\circ)^2)$	92	31.10	27.39

- The position of the assumed GNSS receiver is accurately set.

The detailed result is shown in Figure 11 over the 6 hours of ephemeris. Four types ( $\delta = 2, 4, 6, 8$ ) of building height noise model (mean  $\mu$  equal to zero) are applied. The percentages are shown in Table 6. About 99.07% of the LOS/NLOS classification is obtained. With the increased noise standard deviation, the accuracy decreases gradually. However, even when the building height noise standard deviation reaches 8 m, accuracy still can reach 95.47%.

We can conclude from the result that (a) the building height error can have a slight negative impact against the LOS/NLOS classification, and thus can deteriorate



**FIGURE 11** Relationship between the NLOS detection accuracy and simulated building height error. The simulated building height errors are subject to Gaussian distribution  $N(\mu, \delta^2)$ . The lines represent fitted curves based on the result (in 6 hours) under different error noise models



the performance of the proposed method; (b) a proper way to identify the height of buildings can increase the robustness of the proposed method.

5. Performance sensitivity of the proposed method against yaw (heading) angle errors:

In this paper, the yaw angle is derived by the highly accurate RTK GNSS/INS integrated navigation system. To analyze the performance sensitivity of the proposed method against yaw angle errors, we propose to manually add error noise to the yaw angle. The added error noise is subject to Gaussian distribution ( $\mathcal{N}(\mu, \delta^2)$ ). After posing different noise magnitudes ( $\delta = 2, 4, 6, 8$ ) to the yaw angle, the NLOS detection accuracy is decreased accordingly.

If the yaw angle with noise error model  $N(0, (1^\circ)^2)$  is applied, the performance of the proposed method remains the same. However, the mean positioning error increased from 26.70 to 29.56 m after increasing  $\delta$  to  $2^\circ$ . The NLOS detection accuracy is also reduced to 98.2%. If the  $\delta$  is set as  $4^\circ$  and  $6^\circ$ , the NLOS detection accuracies are decreased to 95.43% and 93.01%, respectively. Meanwhile, the mean positioning errors and standard deviations are slightly increased. We can conclude that the yaw angle error can have a negative impact on the performance of the proposed method (see Table 7).

## 6 | CONCLUSIONS


In this paper, we propose an NLOS correction and improved GNSS positioning method aided by 3D LiDAR. The top boundary of the building is detected using the 3D LiDAR-based point cloud segmentation method, and NLOS satellites are detected based on the detected TEBs. The NLOS are corrected using an NLOS error model, instead of direct exclusion. The GNSS positioning is conducted based on corrected and healthy LOS satellites. The evaluated results show that the proposed method can obtain improved GNSS positioning accuracy when compared to standalone WLS.

The paper proposes to cope with the effects of static buildings on GNSS positioning using 3D LiDAR. In future work, we propose integrating a sky-pointing camera together with LiDAR to correct the NLOS receptions, therefore, improving the GNSS positioning. As the camera captures the sky view in a real-time manner, it will play the role of describing the Skyplot with obstacles and LiDAR is used to provide the distances between the vehicle and the obstacles.

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